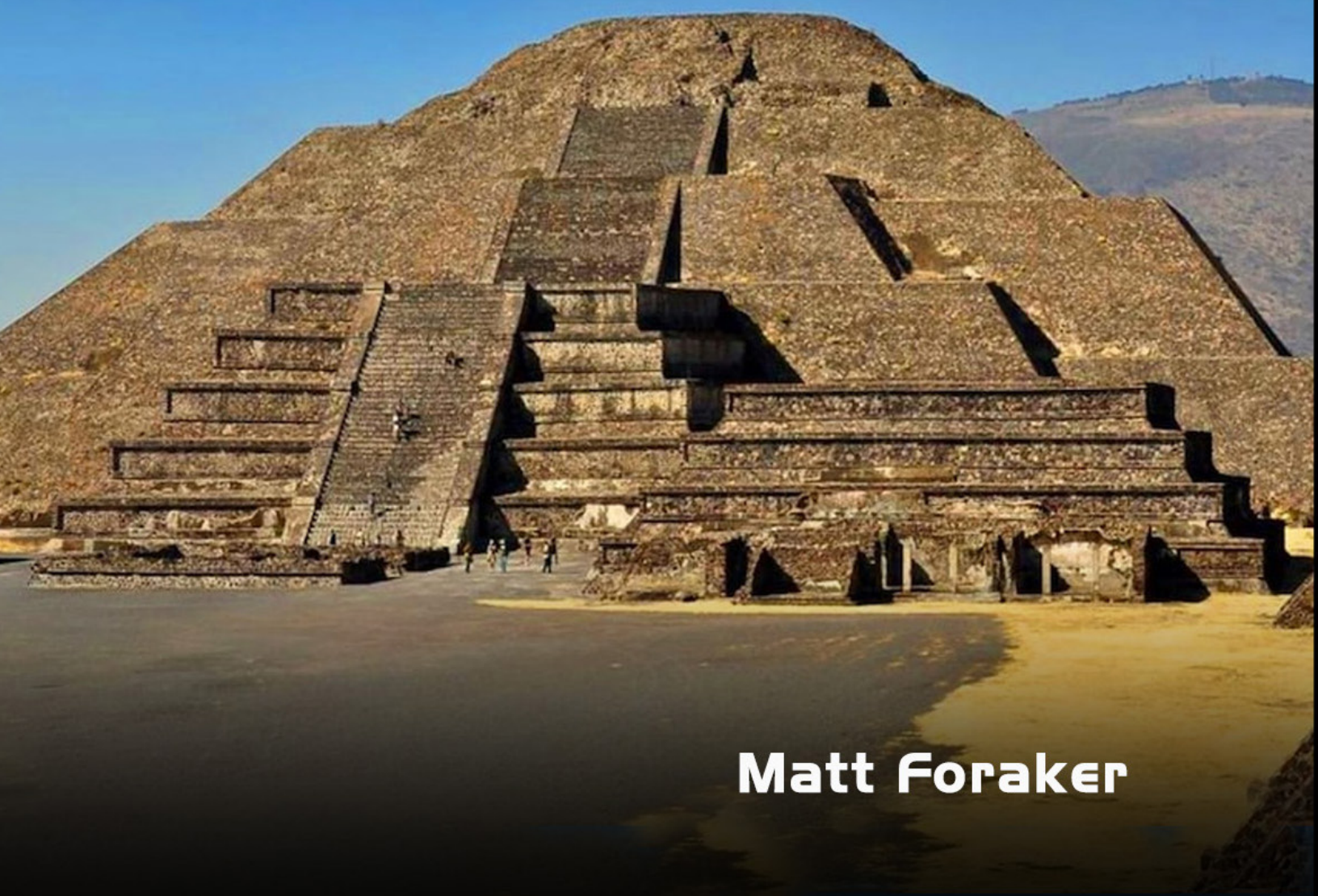




Conceptual Academy

Algebra



Matt Foraker

Conceptual Math

Algebra I



Matt Foraker, Ph.D.
Western Kentucky University
Bowling Green, KY



All inquiries
Support@ConceptualAcademy.com

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Algebra I

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